I want to allow online registration for new customers, but I do NOT want them to be able to enroll into class(es).

You can do that. Follow the instructions on the**Preventing Enrollment** page.